General semi-empirical correlation for condensation of vapor on tubes at different orientations

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A B S T R A C T

Analytical and experimental investigations for condensation of saturated vapor on smooth tube at different orientations are presented. An analytical model was developed starting from mass, momentum and energy equations. The model was solved analytically by the method of characteristics with the aid of a computer program. In the experimental work, heat transfer due to film wise condensation of saturated steam on smooth tube has been investigated for different tube inclinations. Seven series of experiments were conducted at tube inclination angles of 0°, 10°, 20°, 30°, 45°, 60° and 90° with the vertical. Variation of Nusselt number with temperature difference and inclination angles are investigated from the theoretical and experimental results. Both experimental and theoretical results showed the increase of the Nusselt number with the decrease of the temperature difference and the increase of the tube inclination angle from the vertical. Comparison between the experimental and theoretical results showed fair agreement for vertical and horizontal tubes. However, the deviation increased with tilting the tube from horizontal or vertical position. General semi-analytical correlation was deduced from the experimental and theoretical results to fairly predict the Nusselt number for any tube inclination.

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1. Introduction

Tube-side condensation is used in a wide range of engineering applications such as refrigeration, air conditioning, space heating, food industry, automotive and process industries. Nowadays, higher energy efficiency and economic incentive requirements and material saving considerations have increased the need for highly efficient heat transfer surfaces. Heat transfer in tube condensation strongly depends on surface orientation and the enhancement of condensate drainage rate.

Literature review revealed that studies of condensation on vertical and inclined tubes are very limited. In contrast, numerous theoretical and experimental studies were carried out on condensation inside horizontal, vertical and inclined tubes. Many theoretical studies [1–9] were conducted to find the condensate film thickness and condensation heat transfer coefficient at any point in the tube surface in terms of the orientation of the surface and tube surface temperature. The analysis was performed under the same assumptions of Nusselt’s classical theory of film condensation [1].

At the same time, numerous experimental studies were carried out to verify theoretical analysis and obtaining experimental correlations to avoid error in the theoretical analysis due to Nusselt’s assumptions. Hassan and Jakob [2] compared their analytical results with the experimental results for the condensation heat transfer coefficient on inclined cylinder. The experimental results were found to be 28–100% higher than the analytical results. They attributed this deviation due to the rippling of the condensate film that was not taken into account in the theoretical study.

Hussein et al. [3,4] presented theoretical and experimental analysis for wickless heat pipes of different cross section geometries and deduced a correlation for laminar-film condensation heat transfer coefficient in the condenser section of inclined wickless heat pipes flat-plate solar collector. The comparison between theoretical relation and experimental results by other investigators showed a good agreement. Wang and Ma [5] carried out theoretical and experimental studies on condensation inside vertical and inclined thermosyphons tube. They pointed out that no final conclusion can be drawn on the optimum inclination angle at which the maximum heat transfer coefficient can occur. They presented semi-empirical correlations for reflux condensation inside inclined and vertical tubes. Fiedler and Auracher [6] experimentally investigated heat transfer during reflux condensation of
refrigerant R134a in an inclined small diameter tube. They found that the inclination angle has a significant effect on the heat transfer coefficient. Shah [7] presented general modified correlations for condensation inside vertical, inclined and horizontal tubes which can be applied for a wide range of fluid and geometric parameters. Meyer et al. [8] conducted experimental investigation on the effects of the saturation temperature and inclination angle on condensation of R134a flowing inside inclined tubes. The results showed (i) the increase of the heat transfer with the decrease of saturation temperature, and (ii) the existence of optimum inclination angle at which heat transfer is maximum. Wang and Du [9] presented a theoretical study for laminar condensation of R134a and heat transfer.

In the present paper, comprehensive theoretical and experimental investigations of saturated vapor condensing outside tube at different orientations (vertical, horizontal and inclined at different angles of inclination) are presented. The effects of temperature difference, tube inclination angle and tube geometrical parameters are studied. Comparisons between theoretical and experimental results are quantified and investigated. General semi-empirical correlation is suggested for accurate estimation of Nusselt number during condensation on tubes at different orientations.

2. Theoretical analysis

To simplify the mathematical model, some assumptions are considered during the present theoretical analysis. The assumptions are the same of Nusselt [1] assumptions for condensation on vertical surface taking in consideration the effect of the buoyancy force. These assumptions are summarized as follows:

- The flow of the condensate film is laminar, uniform and steady.
- The vapor is considered dry, saturated, pure and free from non-condensable gases.
- The vapor velocity is very small, thus the shear stress at the vapor–liquid interface can be neglected.
Convection heat transfer between the condensate film and the adjacent vapor is neglected and the heat transfer across the condensate film is by conduction.

- The tube surface temperature is uniform.
- The inertia force of the condensate film is neglected and the only force acting on the condensate film is the gravity force.
- Variation of the physical properties of the condensate film and the vapor are neglected.
- The condensate film thickness is negligible with respect to the tube radius.

2.1. Description of condensate motion

The expected path of the condensate film motion on inclined tube is shown in Fig. 1 where the droplet of the condensate film tends to move vertically downwards under the action of gravity, and at the same time the motion is constrained to be in contact with the tube surface. The expected distribution of the condensate film thickness around the surface of the inclined tube is illustrated in Fig. 1. The flow of the condensate film is two dimensional, in the axial and tangential direction, and symmetrical about the plan \( \phi = 0 \). The condensate film thickness is maximum at \( \phi = \pi \) and minimum at \( \phi = 0 \) and increases as the axial distance measured from the top edge of the tube increases.

2.2. Mass conservation

Fig. 2a shows an element of the condensate film on the tube surface. The element is taken at a radial distance \( r \) from the tube surface and ends at the liquid–vapor interface. The mass flow rates of the condensate entering and exit the element in the axial and tangential directions are given by:

\[
\dot{m}_{i,x} = \rho_L \int_0^\delta u_x (D/2 + r) \, d\phi \, dr
\]

(1)

\[
\dot{m}_{o,x} = \dot{m}_{i,x} + \frac{\partial}{\partial x} \left( \dot{m}_{i,x} \right) dx
\]

(2)

\[
\dot{m}_{i,\phi} = \rho_L \int_0^\delta u_x \, dx \, dr
\]

(3)

\[
\dot{m}_{o,\phi} = \dot{m}_{i,\phi} + \frac{\partial}{\partial \phi} \left( \dot{m}_{i,\phi} \right) d\phi
\]

(4)

The net increase in the condensate mass flow rate is

\[
\Delta \dot{m} = (\dot{m}_{o,x} - \dot{m}_{i,x}) + (\dot{m}_{o,\phi} - \dot{m}_{i,\phi})
\]

(5)

Combining Eqns. (1)–(5) and neglecting the condensate film thickness with respect to the tube diameter, it is found that

\[
\Delta \dot{m} = \rho_L \left( \frac{\partial}{\partial x} \int_0^\delta u_x dx + \frac{\partial}{\partial \phi} \int_0^\delta u_x dx \right)
\]

(6)

2.3. Momentum equation

Fig. 2b shows the system of forces acting on the condensate film element. The element is acted by the force of gravity downwards, the buoyancy force upwards and the viscous force components in the axial and tangential directions. As the element is in equilibrium under this system of forces, balances of forces in the tangential and axial directions can be represented by the following equations:
mg \sin \beta \sin \phi = \mu \frac{\partial u_x}{\partial r} (D/2 + r) \, d\phi \, dx \quad (7)

mg \cos \beta = \mu \frac{\partial u_x}{\partial r} (D/2 + r) \, d\phi \, dx \quad (8)

where \( m = \text{mass of the element} - \text{mass of the displaced vapor} \)

\[ m = (\rho_L - \rho_v)(D/2 + r) \, d\phi (\delta - r) \, dx \quad (9) \]

Substituting Eqn. (9) in Eqns. (7) and (8) yields

\[ \mu \frac{\partial u_x}{\partial r} = (\rho_L - \rho_v) g \cos \beta (\delta - r) \quad (10) \]

\[ \mu \frac{\partial u_x}{\partial r} = (\rho_L - \rho_v) g \sin \beta \sin \phi (\delta - r) \quad (11) \]

Integrating Eqns. (10) and (11) under the boundary conditions $u_x = u_\phi = 0$ at $r = 0$ one can get

\[ u_x = (\rho_L - \rho_v) g \cos \beta r (\delta - r/2)/\mu \quad (12) \]

\[ u_\phi = (\rho_L - \rho_v) g \sin \beta \sin \phi r (\delta - r/2)/\mu \quad (13) \]

2.4. Energy equation

Applying energy balance on the studied element given that the rate of heat released during vapor condensation is the same heat conducted across the thickness (\( \delta \)) of the condensate film element [1], i.e.

\[ \frac{k \Delta T}{\delta} (D/2) \, d\phi \, dx = \Delta m h_{fg} \quad (14) \]

Substituting Eqns. (12)–(14) into Eqn. (6), yields

\[ \frac{k \Delta T}{\delta g h_{fg}} = \rho_L \left( \frac{2}{D} \right) \left( \frac{\partial}{\partial \phi} \int_0^\delta \frac{\rho_L - \rho_v}{\mu} \sin \beta \sin \phi (\delta r - r^2/2) \, dr \right) + \frac{\partial}{\partial x} \left( \frac{\rho_L - \rho_v}{\mu} \cos \beta (\delta r - r^2/2) \, dr \right) \quad (15) \]

Integrating the last Eqn. (15) and substituting by

\[ Y = \frac{\delta^2 gh_{fg}(\rho_L - \rho_v) \sin \beta}{3Dk\mu \Delta T} \quad \text{and} \quad Z = \frac{2x}{D \cot \beta} \quad (16) \]

It can be found that

\[ \frac{\partial Y}{\partial Z} + \sin \phi \frac{\partial Y}{\partial \phi} = \frac{4}{3} (1 - Y \cos \phi) \quad (17) \]

Eqn. (17) is a nonlinear first order partial differential equation and its solution gives the condensate film thickness at any point on the surface of the tube. The boundary conditions of this equation is

\[ \delta(x, \phi) = \left( \frac{2Dk\mu \Delta T}{h_{fg}(\rho_L - \rho_v) g \sin \beta} \right)^{1/4} \sin \phi^{-1/3} \left( \int_0^\phi \sin \phi^{1/3} \, d\phi - \int_0^{2 \arctan(e^{-2\tan \phi/2})} \sin \phi^{1/3} \, d\phi \right)^{1/4} \quad (26) \]

that the condensate film thickness equals zero at the upper edge of the tube for any perimeter angle \( \phi \), i.e.

\[ Y(Z, \phi) = 0 \text{ at } Z = 0 \text{ and } 0 \leq \phi < 2\pi \quad (18) \]

Under the boundary condition given by Eqn. (18), Eqn. (17) can be solved analytically by the method of characteristics as described by Smith [20]. Smith showed that the partial differential equation in the form of Eqn. (17) can be obtained by investigating the possibility of finding a direction at each point of the integral surface \( Y = f(Z, \phi) \) along which the partial differential equation is transformed to an ordinary differential equation. This direction is called the characteristics curve. Smith showed that the solution along this characteristics curve is given by

\[ dZ = \frac{d\phi}{\sin \phi} - \frac{dY}{4/3(1 - Y \cos \phi)} \quad (19) \]

The equation of the characteristics curves is given by

\[ dZ = \frac{d\phi}{\sin \phi} \quad (20) \]

Integrating Eqn. (20), gives

\[ e^{-Z} \tan \phi \frac{\phi}{2} = C_1 \quad (21) \]

The solution of Eqn. (19) along these characteristics curves is given by

\[ \frac{d\phi}{\sin \phi} = \frac{dY}{4/3(1 - Y \cos \phi)} \quad (22) \]

Hence,

\[ \frac{dY}{d\phi} + \frac{4}{3} \cot \phi Y = \frac{4}{3} \cosec \phi \quad (23) \]

Eqn. (23) is an ordinary linear first order differential equation. The solution of this equation has the following form as given by Wylie and Barret [21].

\[ Y(Z, \phi) = e^{-\frac{2}{3} \int \cot \phi \, d\phi} \left( \int_0^{\frac{4}{3} \int \cot \phi \, d\phi \, \cosec \phi \, d\phi} + C_2 \right) \quad (24) \]

Conducting the above integration and using the boundary condition \( Y(0, \phi) = 0 \), Eqns. (12) and (24) can be solved together to give

\[ Y(Z, \phi) = \frac{4}{3} \sin \phi^{-4/3} \left( \int_0^\phi \sin \phi^{1/3} \, d\phi - \int_0^{2 \arctan(e^{-2\tan \phi/2})} \sin \phi^{1/3} \, d\phi \right) \quad (25) \]

By substituting Eqn. (16) into Eqn. (25), the condensate film thickness at any point on the tube surface can be expressed in the form

\[ \delta(x, \phi) = \left( \frac{2Dk\mu \Delta T}{h_{fg}(\rho_L - \rho_v) g \sin \beta} \right)^{1/4} \sin \phi^{-1/3} \left( \int_0^\phi \sin \phi^{1/3} \, d\phi - \int_0^{2 \arctan(e^{-2\tan \phi/2})} \sin \phi^{1/3} \, d\phi \right)^{1/4} \quad (26) \]
The local heat transfer coefficient at any point on the tube surface is given by

\[ h(x, \phi) = \frac{k}{\delta(x, \phi)} \]  

(27)

And the average heat transfer coefficient is given by

\[ \overline{h} = \frac{k}{\pi L} \int_0^L \int_0^\infty \delta^{-1}(x, \phi)d\phi dx \]  

(28)

Eqn. (28) gives the average heat transfer coefficient for each tube length and tube diameter in terms of the inclination of the tube with respect to the vertical and the temperature difference between the tube outer surface and the condensing vapor. Integration of Eqn. (26) cannot be obtained analytically, however it can be easily obtained numerically with the aid of a simple computer program.

Eqns. (26)–(28) obtained for vapor condensing outside an inclined tube can be considered as a general equation for vapor condensing on any surface orientations. Nusselt equations for vapor condensing on vertical tube, horizontal tube and inclined flat plat can be derived from Eqns. (26)–(28) by the substitution \( \beta = 0 \), \( \beta = 90 \) and \( D = \infty \), respectively.

3. Experimental setup and procedure

3.1. Experimental setup

A schematic diagram of the experimental setup is shown in Fig. 3. The steam flows from the steam generator (1) to a steam super heater (2) through a steam valve (3) that regulates the steam flow rate. Superheated steam at 1 \(^\circ\)C superheat leaves the super heater and enters the condenser (4). The steam condenses around the condenser tube. The cooling water required for the condenser comes from a constant head tank (5). The condensate exits the condenser via a steam trap (6) to a graduated vessel (7) to measure its mass flow rate. The steam generator is a vertical, electrically heated boiler. Nine electrical heaters, each 3 kW fitted at the lower cover of the steam generator are used to generate saturated steam. The steam generator is fitted with droplet water separator, thermometer, water indicator, pressure gauge, water inlet valve, drain valve and steam exit valve. An electric steam super heater with a power of 1.8 kW is used to eliminate any moisture content carried out with the steam leaving the boiler. The steam super heater raises the temperature of the steam by about 1 \(^\circ\)C above the saturation temperature. The electric power of the steam super heater is controlled by an electric variac to maintain the 1 \(^\circ\)C superheat.

The test section of the experimental setup is the condenser. The condenser is a shell and tube condenser. The condenser shell is made from a steel pipe of 330 mm outer diameter, 2 m length and 6 mm thickness. The test tube (condenser tube) is a stainless tube of 21 mm outer diameter and 1.5 mm thick fitted in the center of the condenser shell. To prevent water vapor from leaving the condenser with the condensate liquid, a steam trap is fitted with the condensate outlet.

The condenser shell is mounted on a mechanism fitted with a protractor to enable changing the inclination angle of the condenser between the vertical and horizontal position as required. To be able to vary the inclination angle, the test section is connected to the cooling water circuit and steam generator section by flexible pressure hoses. The condenser body is thermally insulated with 50 mm glass wall thermal insulation in order to reduce the heat losses from the condenser to the surrounding.

Fifteen K-type thermocouples are embedded on the outer tube at five axial locations, equally distributed along the length of the tube. Each axial location contains three thermocouples distributed at top, bottom and side around the circumference of the test section to be able to measure local wall temperatures (see Fig. 4). The thermocouples leads are embedded and soldered into 0.5 mm deep grooves and taken out through the annulus and fittings. Four other thermocouples are used to measure the cooling water temperature at inlet and exit to the test section and the steam temperatures at exit of steam generator and inlet of the condenser. All thermocouples are calibrated in a constant temperature bath and a measurement accuracy of \( \pm 0.15 \) \(^\circ\)C are obtained. All the temperature signals were acquired using a data acquisition system and sent to a PC for data recording. Two letters graduated vessel is used to collect and measure the condensate during a long period of time, 1–2 min. A stop watch is used to estimate the time of the condensate collection. Accuracy of the eyesight during taking the measurements and unleakage of any condensate were assured. A water flow meter of 1% accuracy is used to measure the cooling water flow rate.

![Fig. 3. Schematic diagram of the experimental setup.](image-url)
3.2. Data reduction

The heat released ($q$) from the vapor during its condensation on the test tube is estimated from the heat gained by the cooling water in the tube and is not calculated from the condensate flow rate. This is to avoid the effects of the of the heat losses from the condenser body and the error in estimating $h_{fg}$ of the steam due to the small variation of steam pressure along test section, purity of water and amount of steam superheat and condensate water subcooled that may occur. Doing so, will reduce the error and uncertainty in estimating the heat transfer coefficient and the Nusselt number.

The heat released ($q$) from the vapor during its condensation is calculated from:

\[ q = \dot{m}_{cw}C_p(T_{cw0} - T_{cw1}) \]  

(29)

To assure the reliability of the experiments, the heat ($q_c$) rejected from the vapor condensing on the test section and on the condenser shell (this part is expected to be very small due to the well thermal insulation of the condenser shell), is estimated from

\[ q_c = \dot{m}_c h_{fg} \]  

(30)

The heat transfer rates $q$ and $q_c$ were determined from both equations (29) and (30). The difference between the two heat flow rates was found to be within 4% for all the experiments and this confirms the reliability of the experiments.

The average condensation heat transfer coefficient on the test tube is calculated from

\[ \overline{h} = \frac{q}{\pi DL(T_w - T_s)} \]  

(31)

The average temperature at any thermocouples station along the tube length is \( [T(\phi = 0) + T(\phi = \pi) + T(\phi = \pi/2) + T(\phi = 3\pi/2)]/4 \). Since the condensate film thickness is symmetric around the plan passing by \( \phi = 0, \phi = \pi \) (see Fig. 1), the condensate film thickness at \( \phi = \pi/2 \) equals to that at \( \phi = 3\pi/2 \) and this makes the temperature at \( \phi = \pi/2 \) equals to that at \( \phi = 3\pi/2 \). For this reason one thermocouple is placed either at \( \phi = \pi/2 \) or at \( \phi = 3\pi/2 \). In the first axial thermocouple station, the thermocouple is placed at \( \phi = \pi/2 \) and in the subsequent axial station it was placed at \( \phi = 3\pi/2 \) and so on. These changes between a thermocouple station and the next are to avoid any error that may come from the nonuniformity of the actual condensate film thickness. Therefore, the average temperature at any axial thermocouple station is calculated from \( [T(\phi = 0) + T(\phi = \pi) + 2T(\phi = \pi/2)]/4 \) or \( [T(\phi = 0) + T(\phi = \pi) + 2T(\phi = 3\pi/2)]/4 \). The overall average tube outer surface temperature is calculated by the arithmetic mean of the average temperature of the five thermocouples stations as follows (see Fig. 4).
The average Nusselt number was normally calculated based on the tube length as the characteristics length of vertical tubes, while it was calculated based on the tube diameter as the characteristics length of horizontal tubes. In this study and for the sake of comparisons, the Nusselt number is calculated based on the tube diameter for all tube orientations as given by:

\[ Nu = \frac{hD}{k} \]  

(33)

Combining Eqns. (29) and (33) together, the expression of \( Nu \) can be put on the form

\[ Nu = f(x_1, x_2, \ldots, x_n) \]  

(34)

where \( x_1 \) to \( x_n \) are all the variables (temperatures, water flow rate, diameter) that affect the experimental determination of \( Nu \). The uncertainty \( \Delta Nu \) in the value of \( Nu \) was estimated based on the procedure of Holman and Gajda [22] and is expressed as follows

\[ \Delta Nu = \sqrt{\sum_{i=1}^{n} \left( \frac{\partial Nu}{\partial x_i} \Delta x_i \right)^2} \]  

(35)

where \( \Delta x_i \) is the uncertainty in the \( x_i \) variable (temperatures, water flow rate, diameter). It was found that the uncertainty for all data of \( Nu \) ranges from 4 to 7 percent.

4. Results and discussions

A simple computer program was developed to numerically evaluate the integrations in Eqns. (26)–(28). The program was run to estimate the Nusselt number for saturated steam condensing outside a tube having a diameter and length of 0.021 m and 2 m, respectively. The program was run for different tube inclination angles \( (\beta = 0, 10, 20, 30, 45, 60 \text{ and } 90^\circ) \) and different temperature differences between the tube outer surface and the saturated steam. Fig. 5 shows the variation of the obtained theoretical average Nusselt number with \( (T_s - T_w) \) at different tube inclinations. Moreover, the results obtained from the experimental data are shown in Fig. 6. Both theoretical and experimental results

![Fig. 5. Variation of theoretical Nusselt number at different inclination angles.](image)

![Fig. 6. Variation of experimental Nusselt number at different inclination angles.](image)

![Fig. 7. Comparison between theoretical, semi-analytical and experimental Nusselt numbers for vertical and horizontal tubes (\( \beta = 0^\circ, 90^\circ \)).](image)
show the increase of Nusselt number with the decrease of the temperature difference and the increase of the tube inclination from the vertical. The increase of the Nusselt number with the decrease of the temperature difference can be attributed to the decrease of the heat transfer rate with the decrease of the temperature difference. Decreasing the heat transfer rate decreases the rate of condensation and consequently decreases the condensate film thickness which decreases the thermal resistance and consequently increases the heat transfer coefficient and Nusselt number. This result agrees well with the previous theoretical and experimental results [1,5,6,8,9,19] for condensation of vapor around surfaces of different geometries and orientations where it was found that Nusselt number increases with the decrease of the temperature difference.
The increase of the Nusselt number with increasing tube inclination from the vertical can be attributed to the behavior of condensate film motion and drainage on the surface of the tube and the path length of the condensate film on the surface of the tube until drainage. The length of the condensate film path until drainage depends on the tube inclination angle. As the tube inclination angle measured from the vertical increases, the path of the condensate film on the tube surface becomes shorter and the rate of condensate drainage increases reducing the amount of the condensate covering the tube surface and consequently decreases the thermal resistance and increases heat transfer coefficient. Fig. 5 reveals that the ratios between the Nusselt numbers of horizontal and vertical tubes obtained from theoretical work is 2.43 which equals to \((L\pi D)^{0.25}\); i.e. the fourth root of the ratio between the condensate film path of the vertical and horizontal tubes. This ratio agrees with the ratio obtained by Nusselt [1]. However, Fig. 6 shows that the ratios between the Nusselt numbers of horizontal and vertical tubes for the different experimental data lie in the range 1.75–3. This deviation can be attributed to the simplified assumptions considered in driving the analytical equations and due to the uncertainty of the experimental work.

The comparison between analytical and experimental results is shown in Fig. 7 for vertical and horizontal tubes and in Fig. 8 for inclined tubes. For vertical and horizontal tubes, Fig. 7 shows that the theoretical results can predict the experimental data with an error of about 10%. This small deviation can be attributed to the simplified assumptions considered in driving the analytical equations and due to the uncertainty of the experimental work. However, Fig. 8 shows that the deviation between the experimental and theoretical results increases with the increase of the inclination angle. This can be attributed to that the effect of the simplified assumptions in the analytical models starts to increase by inclining the tube from the vertical and the horizontal position. Moreover, the actual path of the condensate film motions and the condensate film drainage points may be different than the one considered in the analytical analysis. The theoretical model foresees drainage of the condensate when it reaches the angular position \(\phi = \pi\) but in the actual path the drainage point is generally below this point, so that a thicker (average) condensate film forms, with respect to that theoretically predicted. The large deviation between the experimental and theoretical results agrees well with the results of Hassan and Jakob [2] for the condensation on inclined cylinder where the experimental results were found to be 28–100% higher than the analytical results. They attributed this deviation due to the rippling of the condensate film that is not taken into account in the theoretical study.

To avoid the deviation of the theoretical results in predicting the experimental data, a general semi-analytical correlation was deduced to give the Nusselt number in terms of the physical parameters. The semi-analytical correlation is represented as follows

\[
Nu = C \left( \frac{h_{fg} \rho_l (\rho_l - \rho_s) g}{k_p \Delta T L} \right)^{1/4} D (L/D)^n \left( 1 + \sin^2 25 \beta \right) \tag{36}
\]

where, the constant \((C, n)\) are \((0.985, 0), (0.33, 0.25)\) and \((0.65, 0.791)\) for vertical, horizontal and inclined tubes, respectively.

The results of semi-analytical correlation [Eqn. (36)] are compared with the experimental and analytical results and represented graphically in Figs. 7 and 8. The comparison between results of semi-analytical correlation and all the experimental results is shown in Fig. 9. Fig. 9 shows that the suggested semi-analytical correlation can predict all the experimental data within \(\pm 11\%\).

5. Summary and conclusions

Comprehensive analytical and experimental investigations for condensation of saturated vapor on smooth tubes with different inclination angles are presented. An analytical model was developed starting from mass, momentum and energy equations to give the condensate film thickness and heat transfer coefficient for any tube orientation in terms of the controlling parameters. In the experimental work, heat transfer due to film-wise condensation of saturated steam on inclined smooth tube has been investigated for tube inclination angles of 0°, 10°, 20°, 30°, 45°, 60° and 90° with the vertical. Variation of average heat transfer coefficient and Nusselt number with the temperature difference and inclination angles obtained from theoretical and experimental work are presented, investigated and compared. Both experimental and theoretical results showed the increase of the Nusselt number with the decrease of the temperature difference and the increase of the tube inclination angle from the vertical. Comparison between the experimental and theoretical results showed fair agreement for vertical and horizontal tubes. However, the deviation increased with tilting the tube from horizontal or vertical position. General semi-analytical correlation was deduced from the experimental data and the theoretical results to accurately predict the Nusselt number during vapor condensation on tubes at different orientations.

References


