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# On fuzzy compact spaces

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This chapter is devoted to introduce the information, motivations, ideas, definitions and results about the notions which we shall use throughout the thesis. Chapter 1 -consists of eight sections. In Section 1.2, some information about L-sets and L topological spaces are introduced [16, 39, 55, 63]. In Section 1.3, we recall the definitions and results of the notions of L filters, principal L-filters, L-neighborhood filters and valued L-neighborhood filters presented in [21, 23, 27, 29, 31, 32]. In Chapter 2 we are going to introduce the main notion of this thesis namely, G-compact space, and we study many properties on G-compact spaces. We introduce many kinds of G-compact spaces. In Chapter 3 we are going to introduce a new bi-fuzzy separation axioms which are depending on usual points and ordinary sets. These bi-fuzzy separation axioms will be defined using the notions of L-neighborhood filters at a point and at a set. In Section 1.4, the notion of an L proximity defined by Katsaras in [46, 1 CHAPTER 1. PRELIMINARIES 247, 48] will be recalled. Section 1.5 is devoted to study the relation of the L-uniform spaces defined in [12] with the G-compact spaces. In Section 1.6, we introduce and study the relation of the L-metric spaces defined in [37] with the G-compact spaces. Section 1.7 is devoted to recall a notion of compactness defined in [32], called G-compactness. In Section 1.8, we introduce and study L-separation axioms denoted by  $GT_i$ , ( $i = 0, 1, 2$ ). The information introduced in this section will be the keypoint of the work in the Chapter 3. We defined in Chapter 3 a new bifuzzy separation axioms (  $GT_i$ -spaces ) and defined supra fuzzy topological spaces. For the definitions and results concerning the notions in the classical case which we use throughout the thesis we refer to [15, 17, 26, 45, 51].