
On stability and oscillation of solutions of ordinary differential equation

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In this thesis, we discuss the oscillatory behavior of solutions of the second order neutral delay differential equation of the form $m(r(t)z'(t)) + q(t)f(x(\sigma(t))) = 0$, $t \in [t_0, \infty)$ where $\sigma(t) = t - \tau$ and $\tau \geq 0$. Also, we discuss the oscillation of the second order nonlinear neutral differential equations with deviating arguments of the form $(r(t)(z''(t) \pm f(t, x(\sigma(t)))) = 0$, $t \in [t_0, \infty)$ where $z(t) = x(t) + \sum_{i=1}^n p_i(t)x(\sigma_i(t))$ and $\sigma_i(t) = t - \tau_i$, $\tau_i \geq 0$. Moreover, we investigate the oscillation of the second order nonlinear neutral differential equations of the form $(r(t)(z''(t) + p(t)x(\sigma(t)))) + q(t)f(x(t), x(\sigma(t))) = 0$, $t \in [t_0, \infty)$ where $z(t) = x(t) + \sum_{i=1}^n p_i(t)x(\sigma_i(t))$ and $\sigma_i(t) = t - \tau_i$, $\tau_i \geq 0$. Finally, we discuss the stability character of the second order nonlinear differential equation of the form $x'' + h(t, x) + g(t, x) = 0$, $t \in \mathbb{R}$. The obtained